

Figure 1. Computer-generated thermal ellipsoid plot of 1 . Some important bond distances (angstroms) and angles (degrees) not given in the text or Table I are as follows: $\mathrm{Li}(1)-\mathrm{O}(1 \mathrm{a})=1.962(15), \mathrm{Li}(1)-\mathrm{O}(1 \mathrm{~b})$ $=1.927(22), \mathrm{Li}(2)-\mathrm{O}(2)=1.918(15) ; \mathrm{B}(2)-\mathrm{B}(1)-\mathrm{C}(1)=124.6(4)$, $\mathrm{B}(2)-\mathrm{B}(1)-\mathrm{C}(7)=125.8(6), \mathrm{B}(1)-\mathrm{B}(2)-\mathrm{C}(16)=122.2(6), \mathrm{B}(1)-\mathrm{B}-$ (2) $-\mathrm{C}(25)=128.8(6)$. Interplanar angles between the averaged planes at the following atoms are as follows: $\mathrm{B}(1)$ and $\mathrm{C}(1), 6.3^{\circ} ; \mathrm{B}(1)$ and $\mathrm{C}(7), 86.8^{\circ} ; \mathrm{B}(2)$ and $\mathrm{C}(16), 56.8^{\circ} ; \mathrm{B}(2)$ and $\mathrm{C}(25), 56.6^{\circ}$.

Table I. Selected Bond Distances ( $\AA$ ) and Angles (deg) in 1 and 2

|  | $\mathbf{1}$ | $\mathbf{2}$ |
| :--- | :--- | :--- |
| $\mathbf{B}(1)-\mathrm{B}(2)$ | $1.636(11)$ | $1.706(12)$ |
| $\mathrm{B}(1)-\mathrm{C}(1)$ | $1.613(11)$ | $1.565(12)$ |
| $\mathrm{B}(1)-\mathrm{C}(7)$ | $1.648(7)$ | $1.579(11)$ |
| $\mathrm{B}(2)-\mathrm{C}(16)$ | $1.642(10)$ | $1.576(9)$ |
| $\mathbf{B}(2)-\mathrm{C}(25)$ | $1.643(11)$ | $1.586(12)$ |
| $\mathrm{C}(1)-\mathrm{B}(1)-\mathrm{C}(7)$ | $109.5(5)$ | $115.1(7)$ |
| $\mathrm{C}(10)-\mathrm{B}(2)-\mathrm{C}(25)$ | $108.9(6)$ | $119.8(6)$ |
| angle between $\mathrm{B}(1)$ and $\mathrm{B}(2)$ planes | 7.3 | 79.1 |

alkali metal, $\mathbf{R}=$ organo group) have been structurally characterized to date. The contrast between 1 and the structures of the dimeric lithium salts of alkyls, aryls, amides, phosphides, or alkoxides further emphasizes the unique structural features observed in $1 .{ }^{14}$

Finally, it is notable that calculations ${ }^{15}$ on the parent compound $\mathrm{Li}_{2} \mathrm{~B}_{2} \mathrm{H}_{4}$ show that it is planar and thermodynamically very stable and has a B-B distance of $1.613 \AA$. An alternative configuration, in which the $\mathrm{Li}^{+}$ions are disposed above and below the $\mathrm{B}_{2} \mathrm{H}_{4}{ }^{2-}$ plane, has a B-B distance of $1.629 \AA$ and is $14.9 \mathrm{kcal} \mathrm{mol}^{-1}$ less stable. Clearly, the agreement between the theoretical and structural data for 1 is very good. Further calculations on the energy of the $\pi$-bonding and the rotation barrier in 1 are in progress. ${ }^{16}$

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Supplementary Material Available: Tables of data collection parameters, atom coordinates, bond distances, bond angles, anisotropic thermal parameters, and hydrogen coordinates ( 10 pages); listing of observed and calculated structure factors (17 pages). Ordering information is given on any current masthead page.

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# Three-Dimensional Microscopic ${ }^{1} \mathbf{H}$ NMR Imaging of Rigid Polymers 

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We report the first application of ${ }^{1} \mathrm{H}$ nuclear magnetic resonance (NMR) to obtain three-dimensional (3-D) spatially resolved images of a rigid polymer. The technique, which has been demonstrated on a polycarbonate sample, uses MREV-8 multiple-pulse homonuclear decoupling ${ }^{1,2}$ in combination with 3-D back-projection. ${ }^{3-6}$ The image provides a 3-D map of the proton content within the specimen to a spatial resolution of $150_{x} \times 150_{y} \times 150_{z}$ $\mu \mathrm{m}^{3}$. The reconstructed surface-rendered image is a reasonably accurate reproduction of the specimen's complex topology.

The inherently broad line widths associated with homonuclear dipolar interactions of abundant proton spins in solids have hampered the rapid development of NMR imaging techniques for materials. Only within the last several years have effective imaging strategies been implemented to overcome broadening effects in rigid, protonated solids. Several techniques for proton NMR imaging of solids have been demonstrated, ${ }^{6-15}$ but only in linear (1-D) or planar (2-D) fashion. Spatial discrimination in the third dimension has been difficult to achieve due to the inherently short proton transverse relaxation times ( $T_{2} \mathrm{~s}$ ) in solids. This rapid decay of magnetization has precluded the use of spatial encoding methods, which are commonly used in liquids. ${ }^{16,17}$

Recent work in our laboratory has focused on the use of multiple-pulse coherent averaging of homonuclear broadened lines, which is applied in conjunction with back-projection techniques to obtain 3-D spatially encoded images of proton density. The

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Figure 1. Optical photograph (A, top left), two orientations of the surface-reconstructed 3-D proton image (B and C, bottom left and top right), and a slice from the center of the 3-D image (D, bottom right) of an extruded polycarbonate specimen. 3-D NMR image data were obtained on a Bruker CXP-100 NMR spectrometer fitted with a home-built imaging accessory (described in detail elsewhere ${ }^{20}$ ). Data were collected with 128 data points acquired in nonquadrature mode by the MREV- 8 pulse sequence. A $1.2-\mu \mathrm{s} 90^{\circ}$ pulse was achieved by approximately 200 W of rf with a $3.5-\mathrm{mm}$ solenoidal coil. An interpulse delay time of $3.2 \mu \mathrm{~s}$ was used, giving a total cycle time of $38.4 \mu \mathrm{~s}$. A total of 1600 projections ( $20 \theta$ angles over $\pi / 2$ radians $\times 80 \phi$ angles over $2 \pi$ radians) were acquired with a magnetic field gradient strength of $16 \mathrm{G} / \mathrm{cm}$, and 64 averages were acquired per projection with a recycle delay time of 0.40 s . Data acquisition with these parameters required 12 h . Data were reconstructed on a local Vax-8700 with software written in-house. The final 3-D image was reconstructed with a 3-D Radon inversion code developed at LETI. The 3-D surface-rendered images were rendered, displayed, and photographed from an Ardent/Titan workstation by a commerical image-production package titled Application Visualization System (available from Stardent Computer, Inc.). The slice was additionally processed using a planar $4 \times 4$ median filter. Final resolution was $150_{x}$ $\times 150 y \times 150_{z} \mu \mathrm{~m}^{3}$.

MREV-8 pulse sequence has been applied in the presence of a strong magnetic field gradient (MFG) to generate frequencyencoded 1-D projections of the object space parallel to the MFG vector. A series of projections was acquired by electronically rotating the MFG vector in classical spherical coordinate space about the sample. ${ }^{6}$ The images were subsequently calculated from the series of 1-D phased projections using 3-D Radon transform inversion that was implemented as proposed by Grangeat et al. ${ }^{18}$

An optically transparent, extruded BPA polycarbonate (bisphenol A polycarbonate, Calibre ${ }^{19}$ ) sample with unusual topology was chosen for examination (see Figure 1A). The specimen had a distorted cylindrical geometry ( 3 mm long $\times 2 \mathrm{~mm}$ in diameter) and contained a hole, which had formed during extrusion, along the main axis. The hole measured 400 and $150 \mu \mathrm{~m}$ in diameter at its entrances and was slightly larger in diameter in the specimen's interior.

The MREV-8 sequence narrows the polycarbonate proton line width of the static specimen from 35 to 0.85 kHz . The remaining static line width results from a combination of magnetic suscep-

[^2]tibility effects, chemical shift anisotropy, residual dipolar broadening, and distribution of isotropic chemical shifts. However, it is known that the frequency offset response of the MREV-8 sequence reduces decoupling efficiency as the difference between the decoupling frequency and the observed chemical shift becomes larger. This reduction generates a nonlinear response in amplitude and in observed chemical shift as a function of decoupling frequency. In imaging, where linearity is often required for accurate image reconstruction, these nonlinearities can cause severe artifacts. In an attempt to minimize these effects on image quality, images were acquired by using a moderate MFG strength to limit changes in line widths from 0.85 to 2.0 kHz (chemical shift scaling factor of 2.12 to 2.71 ) across the 1-D projections.

Two orientations of the surface-rendered 3-D proton image of the polycarbonate specimen are presented in Figure 1B,C. A slice taken from a single plane in the center of the specimen is also presented in Figure ID. The major topological features are accurately reproduced in the image, which has a spatial resolution of $150_{x} \times 150_{y} \times 150_{z} \mu \mathrm{~m}^{3}$. The hole is clearly visible in Figure 1C,D, in particular the constriction toward the posterior end of the image. Discontinuous features on the surface represent image artifacts primarily caused by resonance offset effects as discussed above, and to a lesser extent, by 3-D surface-tiling errors caused by poor signal-to-noise ratio. Application of more robust mul-tiple-pulse sequences, such as the 48 -pulse sequence, ${ }^{21}$ may provide
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more efficient line narrowing that leads to higher image resolution and less severe artifacts. Also, development of postprocessing techniques to correct for resonance offset effects is currently underway.
In addition to 3-D mapping of proton density, an immediate extension of this technique is the examination of polymer microstructure (such as cross-link density, homogeneity in blends, and crystallinity) utilizing relaxation ${ }^{22}$ ( $T_{1}$ and $T_{1 p}$ ) and spin-diffusion-weighted image protocols. Direct experimental measurement of morphological changes affected by stress, physical aging, phase transitions, annealing, mechanical and thermal degradation, and oxidation is also possible.

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## Ab Initio Calculations of the Relative Energies of Homocub-1(9)-ene and Homocub-9-ylidene. How Strong Is the Twisted " $\pi$ " Bond in the Olefin? What Is the Ground State of the Carbene?

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Rearrangements of carbenes to olefins are usually highly exothermic and, hence, irreversible reactions. ${ }^{1}$ Nevertheless, bridgehead olefins with sufficient torsional strain are capable of undergoing reversion to carbenes. ${ }^{2}$ The best and most recently studied example of the latter process was discovered by Eaton and Hoffmann in the rearrangement of 9 -phenylhomocub-1(9)-ene (1a) to 1 -phenylhomocub-9-ylidene (2a). ${ }^{3}$ Subsequent investigations in the desphenyl series demonstrated that the olefin (1b) can also be formed from the carbene (2b), ${ }^{4}$ and experiments by Jones, Platz, and co-workers have found the equilibrium constant for this reaction to be approximately unity at room temperature. ${ }^{5}$


1a, $R=P h$
1b, $R=H$

$\mathbf{2 a}, R=P h$
$\mathbf{2 b}, R=H$
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Figure 1. GVB/6-31 G* optimized geometry for $\mathbf{1 b}$, depicting the alignment of the atomic orbitals at $C_{1}$ and $C_{9}$ that results from the pyramidalization at $\mathrm{C}_{9}$.

Table I. Relative Energies Calculated at the GVB/6-31G* Level for Singlets and at the ROHF/6-31G* Level for Triplets

| molecule, state, geometry, symmetry | energy (kcal/mol) |
| :--- | :---: |
| 1b, singlet, equilibrium geometry, $C_{1}$ | 3.8 |
| 1b, singlet, C, planar, $C_{s}$ | 8.2 |
| 1b, triplet, equilibrium geometry, $C_{1}{ }^{a}$ | 5.0 |
| 2b, singlet, equilibrium geometry, $C_{s}{ }^{b}$ | $0^{c}$ |
| 2b, triplet, equilibrium geometry, $C_{2 v}$ | 1.6 |

${ }^{a}$ This geometry, with the hydrogen at $\mathrm{C}_{9} 31.8^{\circ}$ out of the plane defined by $\mathrm{C}_{1}, \mathrm{C}_{8}$, and $\mathrm{C}_{9}$, is lower by $1.4 \mathrm{kcal} / \mathrm{mol}$ than the optimized $C_{5}$ geometry in which the hydrogen at $C_{9}$ lies in this plane. ${ }^{b}$ This geometry, in which $\mathrm{C}_{9}$ is tilted $13.0^{\circ}$ out of the plane defined by $\mathrm{C}_{1}, \mathrm{C}_{5}, \mathrm{C}_{4}$, and $\mathrm{C}_{8}$, is $0.2 \mathrm{kcal} / \mathrm{mol}$ lower in energy than the optimized $C_{2 v}$ structure, in which all five carbons lie in the same plane. ${ }^{c} E=-345.2291$ hartrees.

In this communication we report the results of ab initio calculations on the relative energies of $\mathbf{1 b}$ and $\mathbf{2 b}$. Our calculations not only confirm that $\mathbf{1 b}$ and $\mathbf{2 b}$ are nearly isoenergetic but also they predict that only $4.4 \mathrm{kcal} / \mathrm{mol}$ is required to break the highly twisted " $\pi$ " bond in olefin $\mathbf{1 b}$, and they indicate a singlet ground state for carbene $\mathbf{2 b}$.

GVB calculations that correlate one pair of electrons provide adequate wave functions for the weakly bonding pair of electrons in a deformed alkene ${ }^{6}$ and also for the pair of nonbonding electrons in a singlet carbene. ${ }^{7}$ Therefore the geometries of both 1 lb and 2b were optimized ${ }^{8}$ with GVB-PP(1) calculations, ${ }^{9}$ using both the $3-21 \mathrm{G}^{10}$ and $6-31 \mathrm{G}^{*}$ basis sets. ${ }^{11}$ Vibrational analyses, ${ }^{12}$ per-
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